

# GEOS F493 / F693

## Geodetic Methods and Modeling

### – Lecture 07: InSAR - Making the Interferogram –

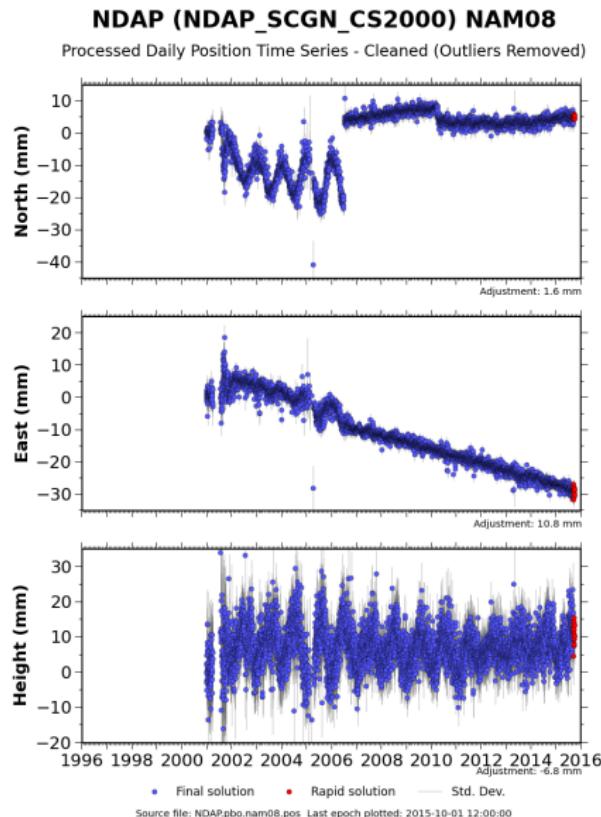
Ronni Grapenthin  
[rgrapenthin@alaska.edu](mailto:rgrapenthin@alaska.edu)

Elvey 413B  
(907) 474-7286

October 14, 2017



# New Segment: “Guess the Process”

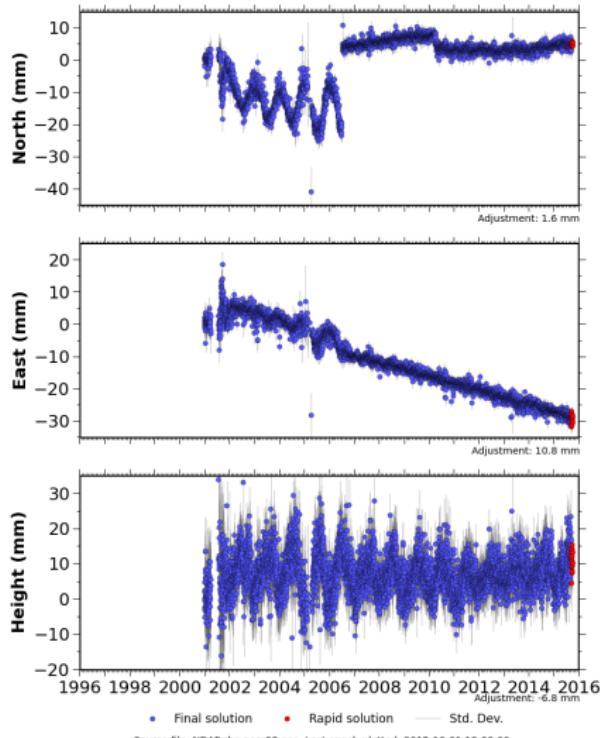


source: UNAVCO

# New Segment: “Guess the Process”

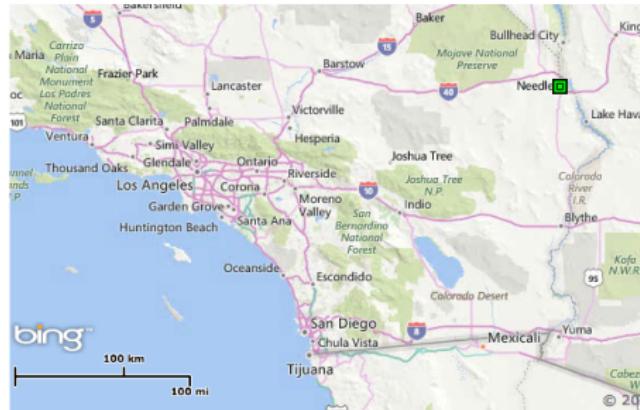
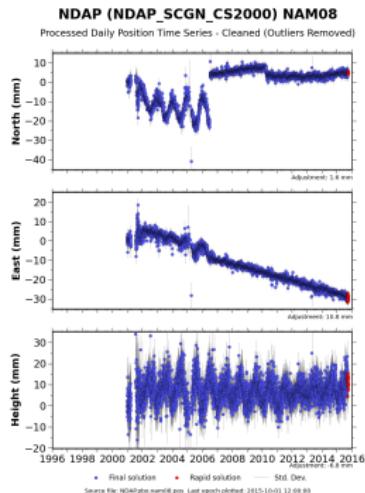
## NDAP (NDAP\_SCGN\_CS2000) NAM08

Processed Daily Position Time Series - Cleaned (Outliers Removed)



source: UNAVCO

# New Segment: “Guess the Process”



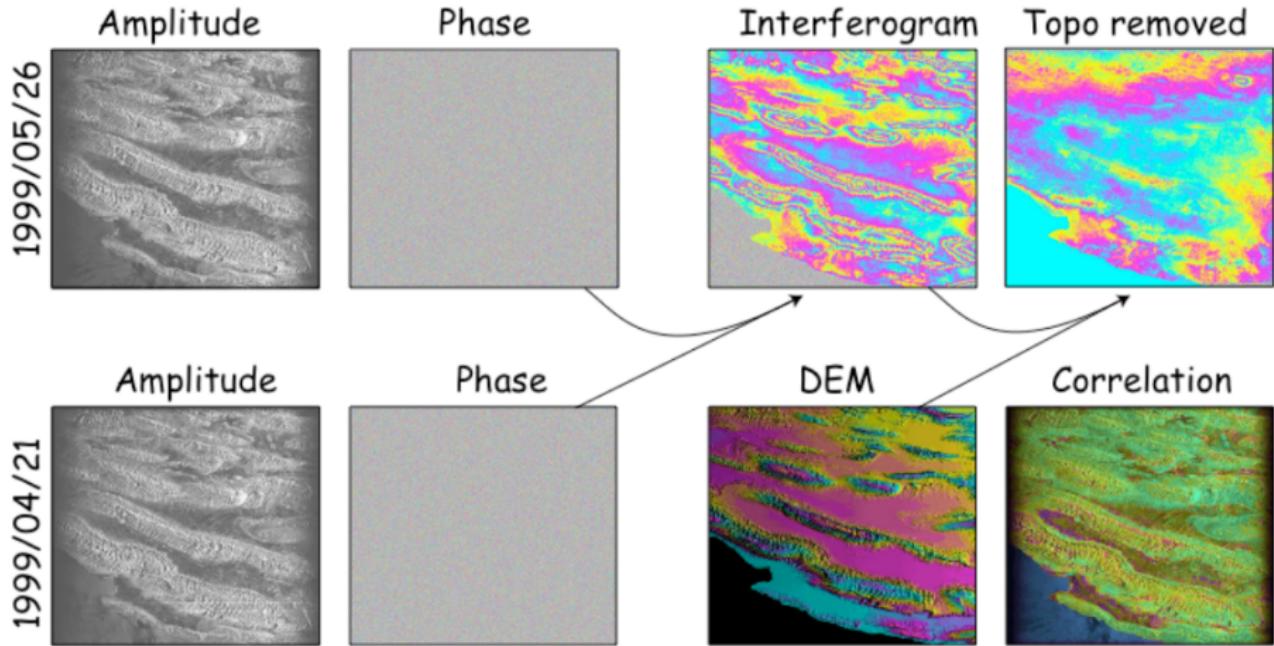
source: UNAVCO

## Equipment and Configuration History

Double-click on a row to see the configuration synopsis for that occupation.

| Start Time        | End Time          | Receiver       | Receiver Serial | Receiver UNAVCO ID | Firmware          | Antenna      | Antenna Serial |
|-------------------|-------------------|----------------|-----------------|--------------------|-------------------|--------------|----------------|
| 2010 Jul 03 00:00 | 2015 Oct 03 23:59 | TRIMBLE NETRS  | 4611206670      | 20811              | 1.3-0             | ASH701945B_M | CR620012201    |
| 2006 Jul 14 16:35 | 2010 Jul 02 23:59 | TRIMBLE NETRS  | 4611206670      | 20811              | 1.1-2 19 Apr 2005 | ASH701945B_M | CR620012201    |
| 2006 Mar 27 18:53 | 2006 Jun 30 23:59 | TRIMBLE NETRS  | 4549261314      | 20069              | 1.1-2 19 Apr 2005 | ASH701945B_M | CR519991876    |
| 2005 Apr 20 01:29 | 2006 Mar 27 17:32 | TRIMBLE NETRS  | 4427235673      | 15582              | 0.3-9             | ASH701945B_M | CR519991876    |
| 2000 Dec 30 00:01 | 2005 Feb 08 23:59 | ASHTECH Z-XII3 | LP03246         | not provided       | CD00              | ASH701945B_M | CR519991876    |

# InSAR - General Concept



loaned from J. Freymueller

# Making an Interferogram

Make interferogram from 2 Single Look Complex images  
(images are in radar coordinates: range  $\rho$ , azimuth  $a$ ):

- 1 align reference and repeat images to sub-pixel accuracy
- 2 multiply complex images (SLC) to form complex interferogram
- 3 extract phase:  $\phi_2 - \phi_1 = \arctan \frac{Im}{Re}$

# Phase Contributors

What's in the phase?

# Phase Contributors

$$\phi = E + \phi_{topo} + D + \epsilon_{orbit} + I + T + \epsilon$$

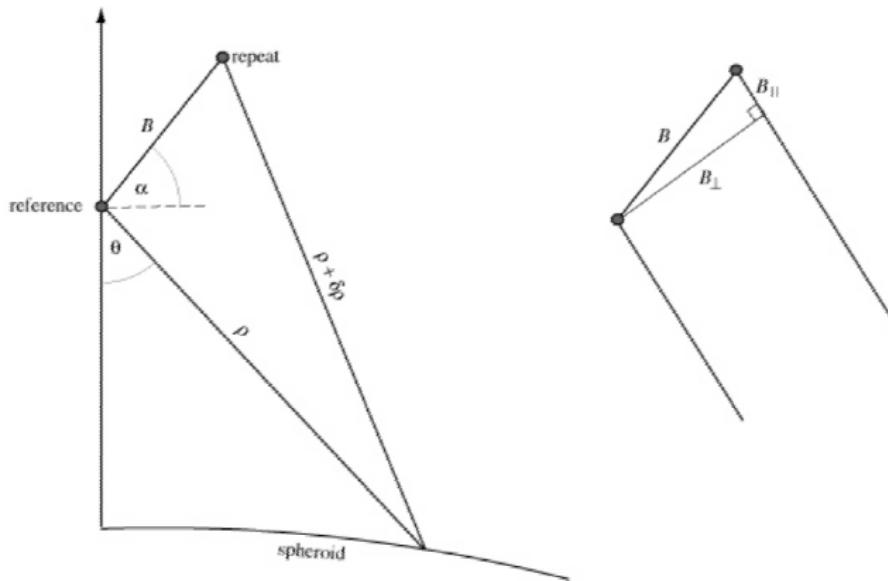
where:

- $E$ : earth curvature (almost planar, known)
- $\phi_{topo}$ : topographic phase (broad spectrum)
- $D$ : **surface deformation (unknown, we want to know!)**
- $\epsilon_{orbit}$ : orbit error (almost a plane, mostly known)
- $I$ : Ionospheric Delay (plane or 40 km wavelength waves!)
- $T$ : Tropospheric Delay (power law, unknown)
- $\epsilon$ : phase noise (white, unknown)

# Correct for Earth's Shape

Earth's shape = curvature + topography

Repeat-pass interferometry geometry:



# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images
- use precise spacecraft orbit to get  $b$  (reference orbit radius),  $B$  (baseline length),  $\alpha$  (baseline orientation)

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images
- use precise spacecraft orbit to get  $b$  (reference orbit radius),  $B$  (baseline length),  $\alpha$  (baseline orientation)
- interpolate topography to each range pixel get look angle from:

$$\theta_{\rho,a} = \cos^{-1} \left[ \frac{(b^2 + \rho^2 - (r_e + t(\rho, a))^2)}{2\rho b} \right]$$

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images
- use precise spacecraft orbit to get  $b$  (reference orbit radius),  $B$  (baseline length),  $\alpha$  (baseline orientation)
- interpolate topography to each range pixel get look angle from:

$$\theta_{\rho,a} = \cos^{-1} \left[ \frac{(b^2 + \rho^2 - (r_e + t(\rho, a))^2)}{2\rho b} \right]$$

- with look angle for each range pixel, calculate phase correction for repeat image:

$$\phi_{\rho,a} = -\frac{4\pi B}{\lambda} \sin(\theta_{\rho,a} - \alpha) + \frac{2\pi B^2}{\lambda\rho} \cos^2(\theta_{\rho,a} - \alpha)$$

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images
- use precise spacecraft orbit to get  $b$  (reference orbit radius),  $B$  (baseline length),  $\alpha$  (baseline orientation)
- interpolate topography to each range pixel get look angle from:

$$\theta_{\rho,a} = \cos^{-1} \left[ \frac{(b^2 + \rho^2 - (r_e + t(\rho, a))^2)}{2\rho b} \right]$$

- with look angle for each range pixel, calculate phase correction for repeat image:

$$\phi_{\rho,a} = -\frac{4\pi B}{\lambda} \sin(\theta_{\rho,a} - \alpha) + \frac{2\pi B^2}{\lambda\rho} \cos^2(\theta_{\rho,a} - \alpha)$$

- multiply  $C_2 C_1^*$

# Topography Correction Algorithm

- map topography from lat, lon, height to radar coordinates and topography over range, azimuth  $t(\rho, a)$
- read row of data from reference and repeat images
- use precise spacecraft orbit to get  $b$  (reference orbit radius),  $B$  (baseline length),  $\alpha$  (baseline orientation)
- interpolate topography to each range pixel get look angle from:

$$\theta_{\rho,a} = \cos^{-1} \left[ \frac{(b^2 + \rho^2 - (r_e + t(\rho, a))^2)}{2\rho b} \right]$$

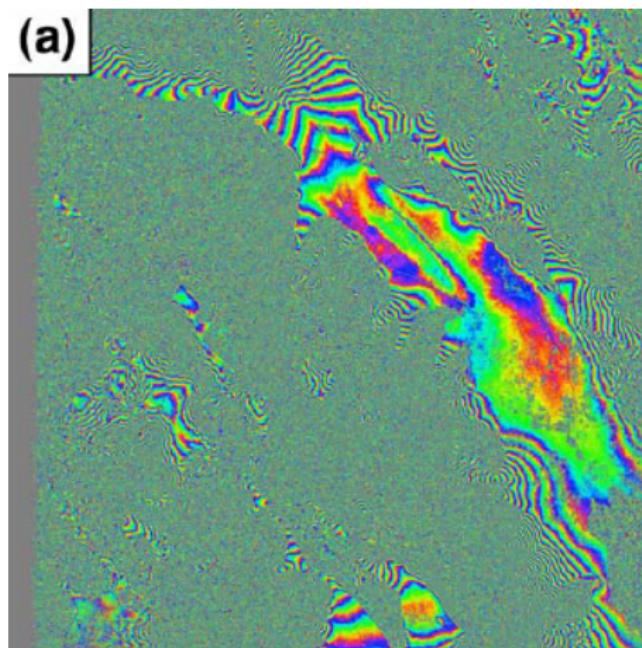
- with look angle for each range pixel, calculate phase correction for repeat image:

$$\phi_{\rho,a} = -\frac{4\pi B}{\lambda} \sin(\theta_{\rho,a} - \alpha) + \frac{2\pi B^2}{\lambda\rho} \cos^2(\theta_{\rho,a} - \alpha)$$

- multiply  $C_2 C_1^*$
- extract phase difference  $\phi_2 - \phi_1 = \arctan(\frac{Im}{Re})$

# Phase due to Topography

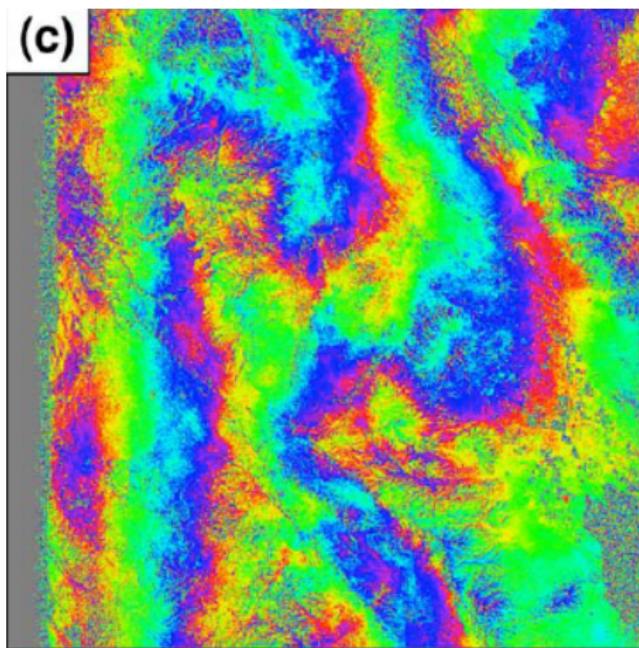
1.95 km baseline Interferogram,  
no topo removed (120 fringes need removal):



Sandwell et al., 2011, GMTSAR documentation

# Phase due to Topography

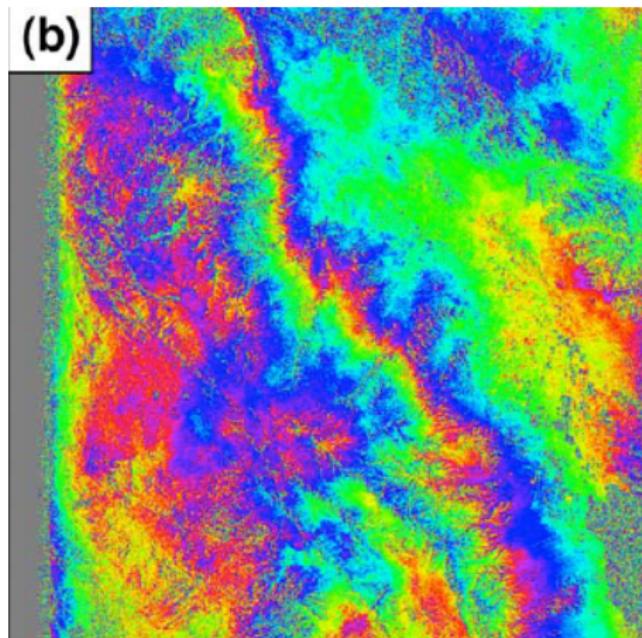
1.95 km baseline Interferogram,  
topography correction using **approximate** formulas:



Sandwell et al., 2011, GMTSAR documentation

# Phase due to Topography

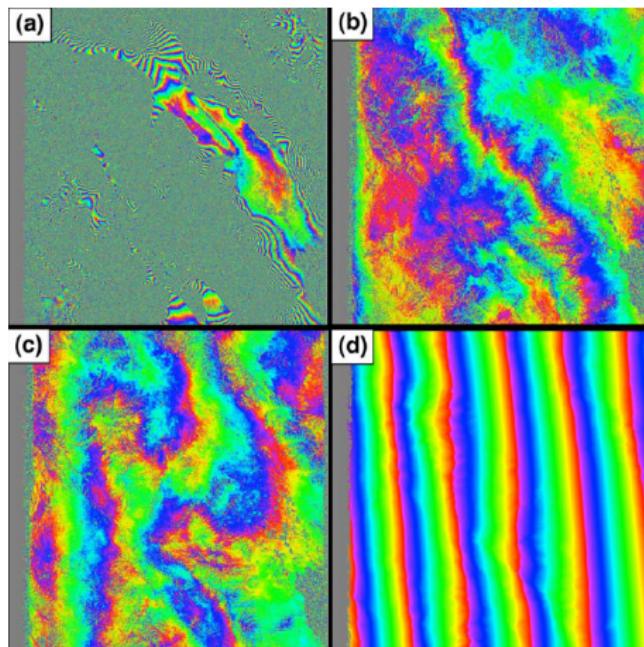
1.95 km baseline Interferogram,  
topography correction using **exact(er)** formulas:



Sandwell et al., 2011, GMTSAR documentation

# Phase due to Topography

1.95 km baseline Interferogram,  
Difference between exact and approx. formulas = 0.6 m ramp



Sandwell et al., 2011, GMTSAR documentation

# Phase due to Topography

In one image

